

Contextual Resource Negotiation-Based Task Allocation and Load Balancing in Complex Software Systems

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Abstract—In the complex software systems, software agents always need to negotiate with other agents within their physical and social contexts when they execute tasks. Obviously, the capacity of a software agent to execute tasks is determined by not only itself but also its contextual agents; thus, the number of tasks allocated on an agent should be directly proportional to its self-owned resources as well as its contextual agents' resources. This paper presents a novel *task allocation* model based on the *contextual resource negotiation*. In the presented task allocation model, while a task comes to the software system, it is first assigned to a principal agent that has high contextual enrichment factor for the required resources; then, the principal agent will negotiate with its contextual agents to execute the assigned task. However, while multiple tasks come to the software system, it is necessary to make load balancing to avoid overconvergence of tasks at certain agents that are rich of contextual resources. Thus, this paper also presents a novel *load balancing* method: if there are overlarge number of tasks queued for a certain agent, the capacities of both the agent itself and its contextual agents to accept new tasks will be reduced. Therefore, in this paper, the task allocation and load balancing are implemented according to the *contextual resource distribution* of agents, which can be well suited for the characteristics of complex software systems; and the presented model can reduce more communication costs between allocated agents than the previous methods based on *self-owned resource distribution* of agents.

Index Terms—Complex software systems, multiagents, contextual resource, negotiation, task allocation, load balancing.

1 INTRODUCTION

Now, many software systems are very complex and have a large number of parts that interact with each other [1]; to manage the complexity of those complex software systems, agent-oriented approaches are well suited for modeling and developing them [2], [3], [4], [5]. With the agent-oriented approaches, the systems always contain many software agents that have many interactions under some organizational constraints and work together to achieve certain objectives occurring through the systems. When a task comes to a complex software system, the software agents in the system should coordinate their activities to implement the task; therefore, coordination among those software agents, which mainly includes two aspects: *task allocation* and *load balancing*, is considered as one of the key concepts to implement tasks effectively in a real complex system [6], [7], [8], [9], [27].

When a multiagent complex system wants to execute a task, the first step is to allocate the task to some software agents, which is called task allocation. The main goal of task allocation is to maximize the overall performance of the system and to fulfill the tasks as soon as possible [6], [7], [8].

Generally, the task allocation in the previous related work is always implemented based on the agents' self-owned resource distribution; the number of allocated tasks on an agent is always directly proportional to its *self-owned resources*, i.e., an agent may be assigned with more tasks if it owns more resources by itself [8], [9], [10], [11].

For example, if agent a_1 holds the resource set $\{r_1, r_2\}$, a_2 holds the resource set $\{r_1\}$, and a task t needs the resource set $\{r_1, r_2, r_3\}$. According to the previous task allocation method based on self-owned resource distribution, a_1 may have higher probability to obtain task t . However, an agent may share resources by negotiating with other agents in the system; now, it is assumed that a_2 can easily share resources $\{r_2, r_3\}$ with its interacting counterparts, but a_1 cannot share any resources from other agents, thus we should allocate task t to agent a_2 but not a_1 . Therefore, in this paper, we present a new idea of task allocation: *if an agent does not own plentiful resources by itself, but it can obtain enough resources from other interacting agents easily, it may also be allocated tasks; the number of allocated tasks on an agent is directly proportional to not only its own resources but also the resources of its interacting agents*.

The complex software systems are always modeled both from physical and social viewpoints. Generally, each agent locates at a physical place and has some physically interacting agents in the complex system; on the other hand, the complex systems are built on the socially organized multiagents, thus each software agent also locates in some social organizations [12], [13], [14], [15]. Therefore, each agent in the complex system may have two kinds of contexts, one is the physical context, and the other is the social context [16], [17], [18]. The resources owned by the agents within the contexts of an agent are called contextual resources. Obviously, agents will often negotiate

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Manuscript received 20 June 2007; revised 1 Dec. 2007; accepted 25 June 2008; published online 21 July 2008.

Recommended for acceptance by R. Eigenmann.

For information on obtaining reprints of this article, please send e-mail to: tpsds@computer.org, and reference IEEECS Log Number TPDS-2007-06-0200. Digital Object Identifier no. 10.1109/TPDS.2008.133.

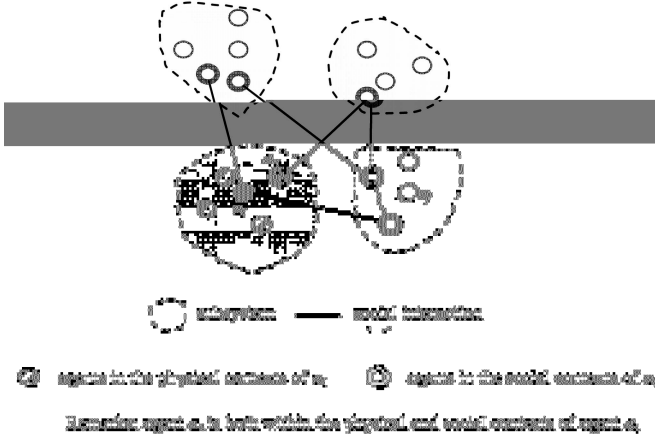


Fig. 1. An example to demonstrate the physical and social contexts in the complex system.

with the agents within their physical and social contexts when they execute tasks. Therefore, our idea of the task allocation in complex software systems can also be explained as follows: *the number of allocated tasks on an agent is directly proportional to not only its self-owned resources but also the resources of its contextual agents; the task allocation of system should be determined by the contextual resources distribution of agents.*

Fig. 1 shows those two kinds of contexts of agents in a complex system, where the subsystem is considered as the physical context and the set of organizationally interacting agents is considered as the social context. We let the set of resources owned by a_i be $\{r_1, r_2\}$ and the set of resources owned by a_j be $\{r_1, r_2, r_3\}$. Now, it is assumed that a task needs the resources $\{r_1, r_2, r_3, r_4\}$; if we make task allocation based on self-owned resources, a_j will have higher probability to obtain the task since it can satisfy the resource requirement of the task better than a_i . However, now a_* is within the context of a_i and has the resources $\{r_3, r_4\}$; thus, we can suggest that a_i has higher probability to obtain the task since a_i can obtain the resources easily by negotiating with a_* .

As said above, if an agent possesses more contextual resources, it may be assigned more tasks accordingly. However, if too many tasks are crowded on certain agents that are rich of contextual resources, then the tasks may be delayed and do not obtain quick responses; therefore, we should let some tasks be switched to other agents with relatively fewer contextual resources but lower task loads, which is called *load balancing*. In the related work about load balancing [10], [11], [19], [20], [21], [22], the number of tasks queuing for an agent is the determinative factor for such agent's right in the future task allocation; if there are too many tasks queuing for an agent, the probability of such agent to obtain new tasks will be reduced.

Since every agent is located within some contexts and will negotiate with its contextual agents to borrow resources for executing tasks, therefore, in this paper, we will develop the load balancing method also based on the contextual resource distribution: *if an agent, a , is allocated with too many tasks, then it is not only a itself but also the agents in the context of a should be reduced the possibilities to accept new tasks in the future.*

The main novelty of this paper is that it presents a novel model for task allocation and load balancing based on the contextual resource negotiation but not the self-owned

resource distribution among software agents; therefore, our model can be well suited for the characteristics of complex software systems. The rest of this paper is organized as follows: In Section 2, we describe the contextual resource negotiation in complex software systems; in Section 3, we present the task allocation model to meet the contextual resource distribution of complex software systems; in Section 4, we address the context-associated load balancing for multiple tasks; in Section 5, we provide the simulation results to validate our proposed model; in Section 6, we present some discussions on the extension of our model. Finally, we conclude this paper in Section 7.

2 CONTEXTUAL RESOURCE NEGOTIATION

The context of an agent can be simply regarded as the environment it is situated [26], which includes the physical context and the social context (organizational one). The physical context is produced by the agent's physical environment, which can be regarded as the agent's physical location, and the physically nearby agents within the subsystem; the resources owned by the agents within its physical context are called the *physically contextual resources*. On the other hand, agents in the complex system should be organized within some social organizations [12], so the counterpart agents in the social organizations can be regarded as the agent's social context, and the resources of the agents in the social context are called *socially contextual resource*.

2.1 Physically Contextual Resource

If an agent lacks the necessary resources to implement the allocated task (we call such agent as *initiator agent*), it may negotiate with its physically contextual agents; if the physically contextual agents have the required resources (we call those agents that lend resources to the initiator agent as *response agents*), then the initiator agent and the response agents will cooperate together to implement such task.

Then, which ones will the initiator agent negotiate with? To minimize the negotiation communication costs, the initiator agent can implement the negotiation process from near agents to far agents gradually within the physical environment.

The negotiation relations from agent a to other agents within its physical context form a directed acyclic graph with single source a , which is called the physically contextual resource negotiation topology (PCR-NT) of agent a .

Definition 1. PCR-NT. A PCR-NT of agent a is a directed acyclic graph with single source a , the agents in the graph are the ones negotiated by agent a , and the path length from a to any other agent is the physical negotiation gradation of that agent.

Definition 2. Physical negotiation gradation. Let a be an agent that will negotiate with other agents within its physical context and the agents in the n th round of negotiation of agent a be called the physical contexts with gradation n .

Let a_i be the initiator agent, and the resources owned by a_i be $\mathbf{R}_{a_i}$; now, task t is allocated to a_i , and the set of requested resources for implementing t is $\mathbf{R}_t$. Therefore, the set of lacking resources of a_i to implement t is $\mathbf{R}_{a_i}^t$:

$$\mathbf{R}_{a_i}^t = \mathbf{R}_t - \mathbf{R}_{a_i}. \quad (1)$$

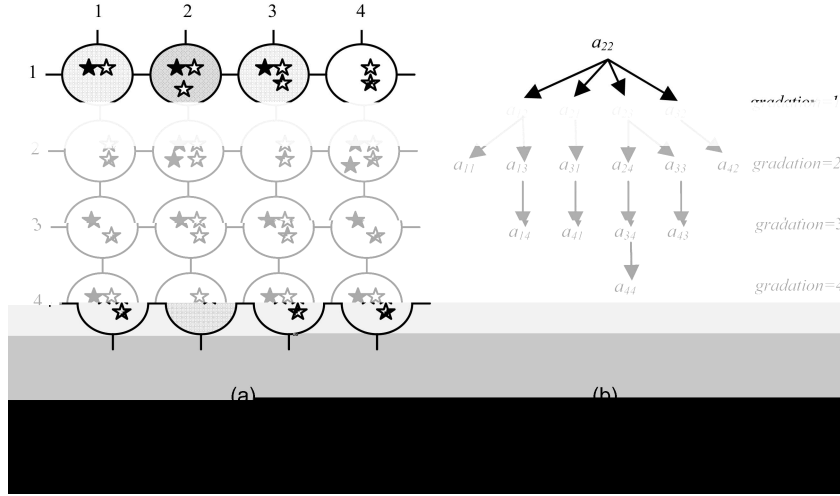


Fig. 2. An example for constructing the PCR-NT.

Now, it is assumed that agent a_j is negotiated by a_i , the set of resources owned by a_j is $\mathbf{P}_{a_j}$. If a_j has any resources that are requested by a_i to implement t , then the set of resources that a_j can lend to a_i for implementing task t is

$$\mathbf{P}_{a_j \rightarrow a_i}^t = \{r | r \in \mathbf{P}_{a_j} \wedge r \in \mathbf{P}_{a_i}^t\}. \quad (2)$$

Thus, the set of lacking resources of a_i to implement t will be reduced as

$$\mathbf{P}_{a_i}^t = \mathbf{P}_{a_i}^t - \mathbf{P}_{a_j \rightarrow a_i}^t = \mathbf{P}_{a_i}^t - \mathbf{P}_{a_j}. \quad (3)$$

The initiator agent a_i will negotiate with the physically contextual agents according to the PCR-NT, until all requested resources are satisfied. The negotiation process is shown as Algorithm 1.

Algorithm 1. Physically contextual resource negotiation of agent a :

- ```
// a is the initiator agent, A is the physical context of a //
1) Set the tags for all agents in A to 0 initially;
2) Create Queue(Q);
3) Insert Queue(Q, a);
4) Set the tag of a to 1;
5) b = 0;
6) A_t = {a}; /*The allocated agent set for task t*/
7) P_a^t = P_t - P_a; /*The lacking resources of agent a to implement task t*/
8) If P_a^t == {}, then b = 1; /*Agent a can provide all resources to implement task t*/
9) While ((!EmptyQueue(Q)) and (b == 0)) do:
 9.1) aout = Out Queue(Q);
 9.2) P' = P_a^t - P_aout;
 9.3) If P' != P_a^t, then: /*Agent aout can satisfy some requests of a*/
 9.3.1) P_a^t = P_a^t - P_aout; /*Agent a obtains resources from aout to implement t*/
 9.3.2) A_t = A_t ∪ {aout};
 9.4) If P_a^t == {}, then b = 1; /*All resources for implementing t are satisfied*/
 9.5) For ∀alocal ∈ L_aout: /*L_aout is the set of all physical neighbors of aout*/
```

if the tag of alocal is 0, then: /\*If agent alocal was not negotiated by a before\*/

9.5.1) Insert Queue(Q, alocal);

9.5.2) Set the tag of alocal to 1;

10) If (b == 1), then Return (A\_t) /\*All resources for implementing t are satisfied\*/

else Return (False);

11) End.

**Theorem 1.** If all resources for implementing task  $t$  can be satisfied by using Algorithm 1, the total communication cost between the initiator agent and the physically response agents is the minimum.

**Proof.** Let  $a_i$  be the initiator agent and the set of lacking resources of  $a_i$  to implement  $t$  be  $\mathbf{P}_{a_i}^t$ . If Algorithm 1 is used, the set of response agents is  $A_*$  ( $A_* = A_t - a_i$ ), and the total communication cost between  $a_i$  and  $A_*$  is  $C_*$ . Now, if there is a set of agents  $A'_*$ ,  $A'_* \neq A_*$ , which can provide  $\mathbf{P}_{a_i}^t$ , and the total communication cost between  $a_i$  and  $A'_*$  is  $C'_*$ ; if  $C'_* < C_*$ , it denotes that there are any agents with higher gradations that provide the required resources in  $\mathbf{P}_{a_i}^t$ , but the lower gradation agents with required resources do not provide the required resources in  $\mathbf{P}_{a_i}^t$ . Obviously, such situation cannot take place in Algorithm 1. Therefore, we have Theorem 1.  $\square$

**Example 1.** Fig. 2 is an example for constructing the PCR-NT, where  $a_{22}$  is the initiator agent. In Fig. 2, the set of resources owned by agent  $a_{22}$  is  $\{r_1, r_2, r_3, r_3\}$ . Now, we let a task  $t$  be allocated to  $a_{22}$ , and the resources requested by  $t$  be  $\{r_1, r_1, r_2, r_2, r_3, r_3, r_3, r_3\}$ ; obviously,  $a_{22}$  lacks the resources  $\{r_1, r_2, r_3, r_3\}$ . At first,  $a_{22}$  negotiates with  $a_{12}$  and obtains the requested resources  $\{r_1, r_3\}$ ; second,  $a_{22}$  negotiates with  $a_{21}$  and obtains the requested resources  $\{r_2\}$ ; third,  $a_{22}$  negotiates with  $a_{23}$  but obtains no requested resources; at last,  $a_{22}$  negotiates with  $a_{32}$  and obtains the requested resources  $\{r_3\}$ ; now, the requested resources of  $a_{22}$  to implement  $t$  are all satisfied. Therefore, the agents  $\{a_{22}, a_{12}, a_{21}, a_{32}\}$  will implement task  $t$  corporately. The negotiation process is shown in Fig. 3.

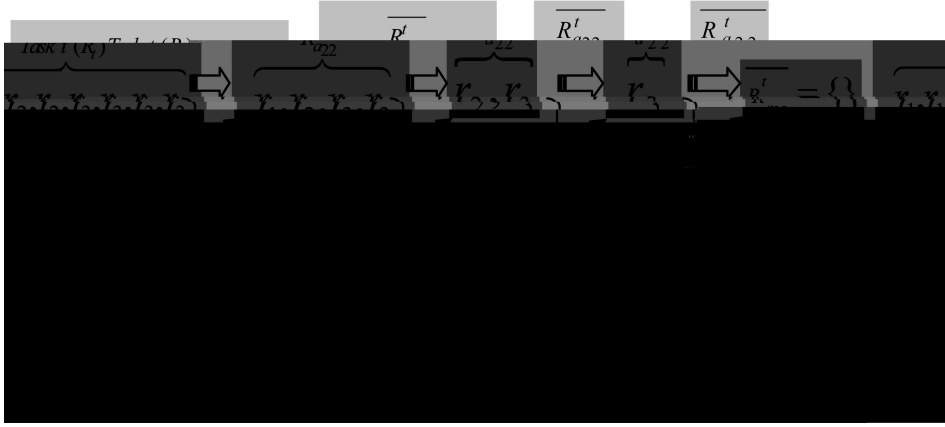


Fig. 3. Physically contextual resource negotiation process of the example in Fig. 2.

## 2.2 Socially Contextual Resource

The complex systems can be modeled as the multiagents organized within certain social structures [14], [23]. With the social organizations, the social interaction relations describe the obligations and structures among agents in the complex systems [13]. Agents will always interact and negotiate with other agents within the social contexts while they execute tasks.

In the social organizations, it is more likely that the near individuals may have more similarities and, being closer together in the organizational hierarchy, share more common interests than the remote individuals [24]. Therefore, in the social organizations of complex systems, each agent will negotiate with other agents for the requested resources gradually from near places to remote places.

The hierarchical structure is a typical social organization, thus first we address the negotiation of social contextual resources within hierarchical structures; after that, we will address the one within arbitrary social structures.

In the social contexts, the agents negotiate with other agents also according to certain topologies. Referring to Definitions 1 and 2, we now give the definitions of social negotiation gradation and socially contextual resource negotiation topology (SCR-NT).

**Definition 3.** Social negotiation gradation. Let  $a$  be an agent that will negotiate with other agents within its social context and the agents in the  $n$ th round of negotiation of agent  $a$  be called the social contexts with gradation  $n$ .

**Definition 4.** SCR-NT. An SCR-NT of agent  $a$  is a directed acyclic graph with single source  $a$ , the agents in the graph are the ones negotiated by agent  $a$ , and the path length from  $a$  to any other agent is the social negotiation gradation of that agent.

### 2.2.1 Hierarchical Structure

In the hierarchical structures, each agent can interact *directly* only to its superiors and subordinates; thus, each agent will first negotiate with its superiors or subordinates for resources. Moreover, in the hierarchical organizations, resource negotiation always happens between pairs of agents that share the same immediate superior; and agents will always negotiate resources through the lowest common ancestor [25]. Therefore, let there be an agent  $a$  that can negotiate with other agents within the hierarchical structure according to the following orders:

1. the subordinates of agent  $a$  in the hierarchical structure;
2. the immediate superior of agent  $a$ ;
3. the sibling agents with the lowest common superiors.

**Example 2.** In Fig. 4, let agent  $a_{21}$  be the initiator agent, we can see the construction of an SCR-NT according to the above social negotiation orders in the hierarchical structure.

Let  $a$  be the initiator agent, and the set of agents in  $a$ 's social context be  $A$ , now the socially contextual resource negotiation process of agent  $a$  in hierarchical structures is shown as Algorithm 2.

**Algorithm 2.** Socially contextual resource negotiation of agent  $a$  in a hierarchical social structure.

*/\*  $T_x$ : the subtree whose root is agent  $x$  in the hierarchical structure;  $p_x$ : the parent node of  $x$  in the hierarchical structure. \*/*

- 1) Set the tags for all agents in  $A$  to 0 initially;
- 2)  $b = 0$ ;
- 3)  $A_t = \{a\}$ ; */\*The allocated agent set for task  $t^*$ \*/*
- 4)  $\bar{R}_a^t = \bar{R}_t - \bar{R}_a$ ; */\*The lacking resources of agent  $a$  to implement task  $t^*$ \*/*
- 5) If  $\bar{R}_a^t == \{\}$ , then  $b = 1$ ; */\*Agent  $a$  can provide all resources to implement task  $t^*$ \*/*
- 6) If  $(b == 0)$ , then:
  - 6.1) **Negotiation** ( $a, a$ ); */\* $a$  negotiates with the agents within  $T_a$  by calling Algorithm 3\*/*
  - 6.2)  $atemp = a$ ;
  - 6.3) **While**  $((b == 0) \text{ and } (p_{atemp} \neq Nil))$  **do**:
    - 6.3.1)  $atemp = p_{atemp}$ ;
    - 6.3.2) **Negotiation** ( $a, atemp$ ); */\* $a$  negotiates with the agents within  $T_{atemp}$  by calling Algorithm 3\*/*
- 7) If  $(b == 1)$ , then **Return** ( $A_t$ ) */\*All resources for implementing  $t$  are satisfied\*/* **else Return** (False);
- 8) **End**.

We can use the lay-based traversal method in tree to implement the negotiation process in Algorithm 2. The method is shown as Algorithm 3.

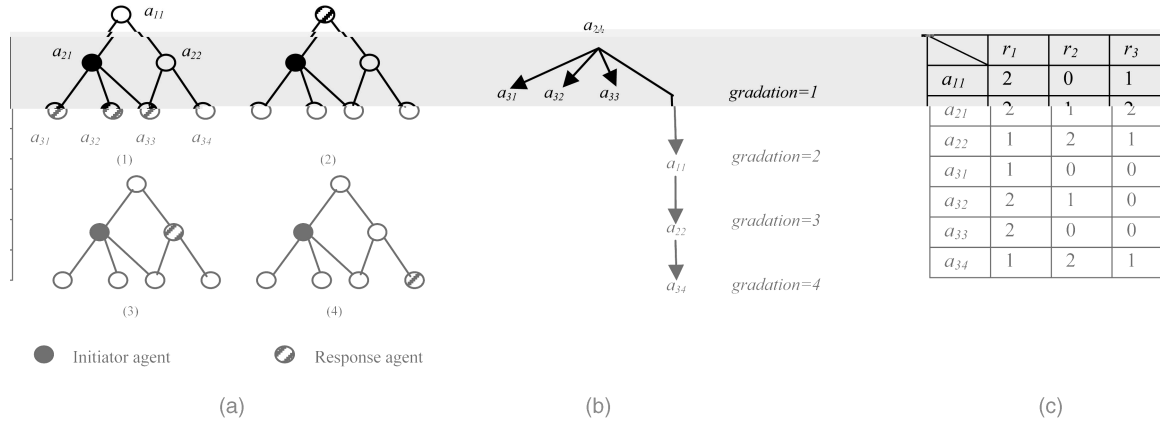


Fig. 4. An example for constructing the  $\text{SCR-NT}$  in a hierarchical social structure; now, it is assumed that  $a_{21}$  is the initiator agent. (a) Negotiation topology evolution. (b)  $\text{SCR-NT}$  of  $a_{21}$ . (c) The number of resources owned by agents.

**Algorithm 3. Negotiation** ( $a, x$ ). /\* Agent  $a$  negotiates with the agents in subtree  $T_x$  \*/

- 1) **Create** Queue ( $Q$ );
- 2) **Insert** Queue ( $Q, x$ );
- 3) **Set** the tag of  $x$  to 1;
- 4) **While** (!EmptyQueue( $Q$ ) and ( $b == 0$ )) **do**:
  - 4.1)  $a_{out} = \text{Out Queue}(Q)$ ;
  - 4.2)  $\bar{R}' = \bar{R}_a^t - \bar{R}_{a_{out}}^t$ ;
  - 4.3) **If**  $\bar{R}' \neq \bar{R}_a^t$  **then**:
    - 4.3.1)  $\bar{R}_a^t = \bar{R}_a^t - \bar{R}_{a_{out}}^t$ ; /\* Agent  $a$  obtains resources from  $a_{out}$  to implement  $t$  \*/
    - 4.3.2)  $A_t = A_t \cup \{a_{out}\}$ ;
  - 4.4) **If**  $\bar{R}_a^t == \{\}$ , **then**  $b = 1$ ; /\* All resources for implementing  $t$  are satisfied \*/
  - 4.5) **For**  $\forall \text{achild} \in \text{child}(a_{out})$ :
    - If** the tag of  $\text{achild}$  is 0:
      - 4.5.1) **Insert** Queue( $Q, \text{achild}$ );
      - 4.5.2) **Set** the tag of  $\text{achild}$  to 1;
- 5) **Return** ( $b$ );
- 6) **End**.

Obviously, with Algorithms 2 and 3, we can constrain the resource negotiation process in hierarchical social structures as follows:

**Lemma 1.** *If all resources for implementing task  $t$  can be satisfied by using Algorithms 2 and 3, the set of socially response agents in hierarchical social structure can satisfy one of the following*

situations: 1) all response agents are located in the subtree of the initiator agent or 2) the ancestor between the initiator agent and all response agents is the lowest.

According to the information exchange criterion in [25], our presented resource negotiation method can also have higher probability to reduce the communication cost compared to other random negotiation processes. Thus, we can obtain the good performance for resource negotiation, which is also tested by our simulation tests in Section 5.

**Example 2 (continue).** In Fig. 4, the set of resources owned by agent  $a_{21}$  is  $\{r_1, r_1, r_2, r_3, r_3\}$ . Now, a task  $t$  is allocated to  $a_{21}$ , and the resources requested by task  $t$  is  $\{r_1, r_1, r_2, r_2, r_3, r_3, r_3, r_3\}$ ; obviously,  $a_{21}$  lacks the resources  $\{r_2, r_3, r_3\}$ . The negotiation process is shown in Fig. 5.

## 2.2.2 Arbitrary Structure

There are always two kinds of arbitrary social structures in the complex systems, one is the directed structure where agent interaction relation is unilateral, and the other is the undirected structure where agent interaction relation is bidirectional.

To minimize the negotiation communication time, we can make an agent negotiate with other agents for the requested resources based on the Breadth-First Traversal method in the

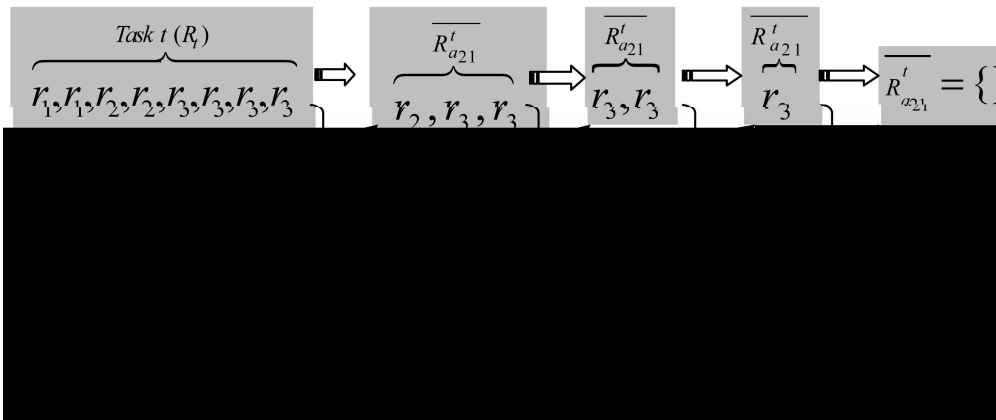


Fig. 5. Socially contextual resource negotiation process of the example in Fig. 4.

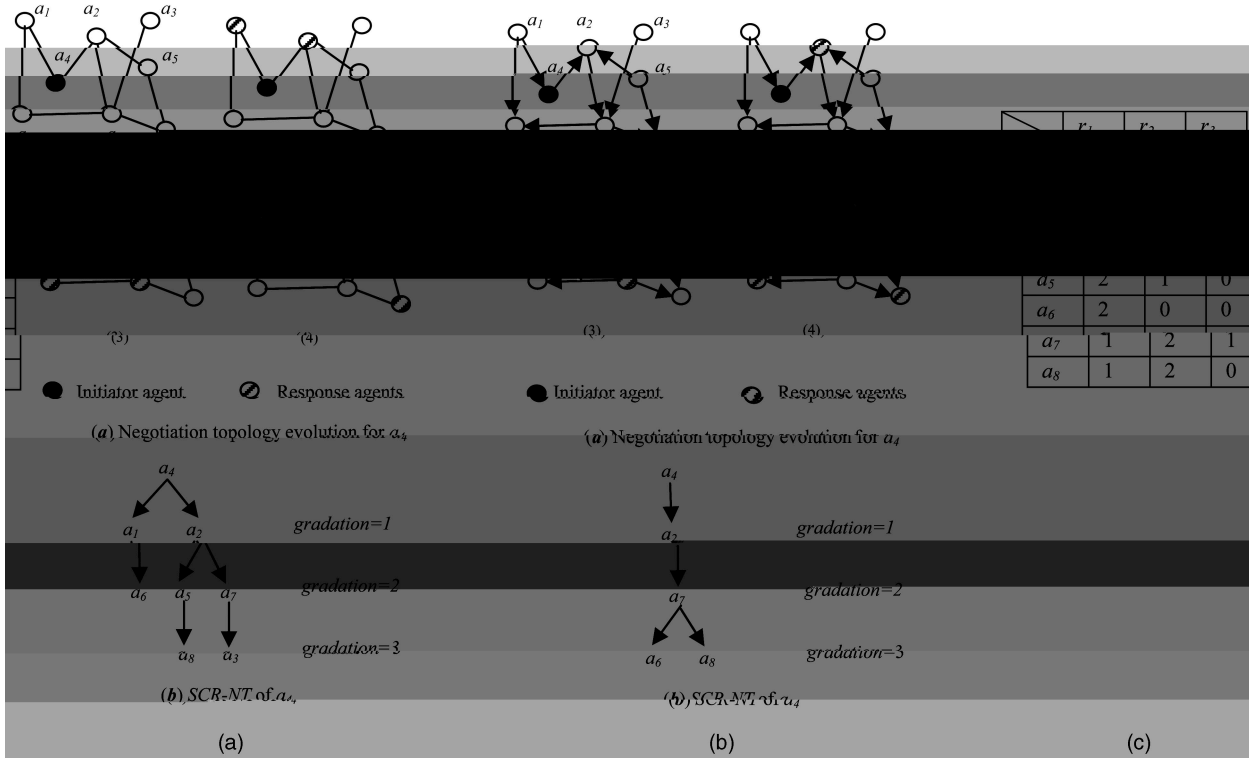


Fig. 6. An example for constructing the SCR-NT in arbitrary social structure. (a) Undirected arbitrary social structure. (b) Directed arbitrary social structure. (c) The number of resources owned by the agents.

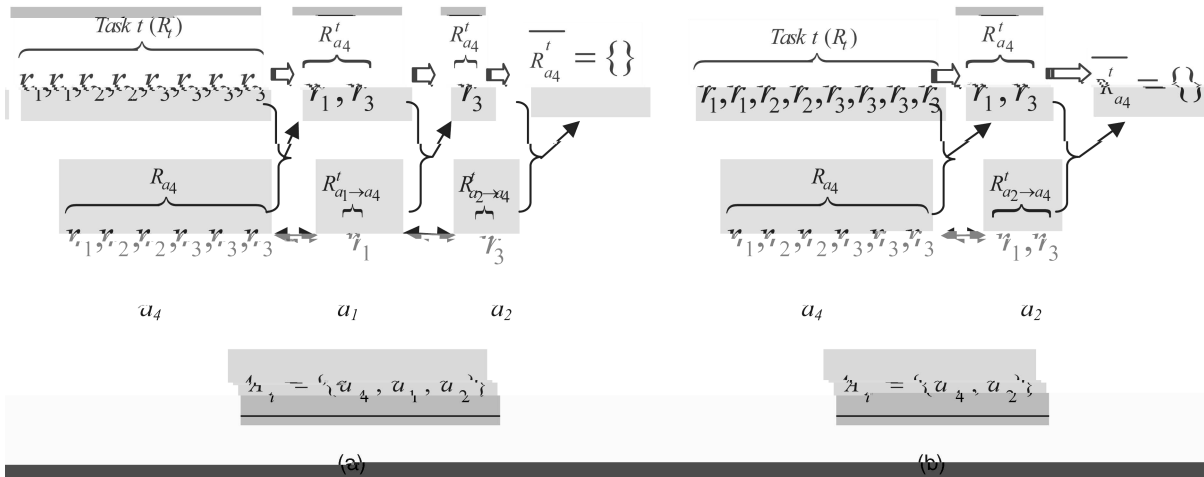


Fig. 7. Socially contextual resource negotiation process of the example in Fig. 6.

graph. The algorithm for the negotiation process within arbitrary social structure is the same as Algorithm 1.

**Theorem 2.** If all resources for implementing task  $t$  can be satisfied by using our algorithm, the total communication cost between the initiator agent and the socially response agents in arbitrary social structure is the minimum.

**Proof.** The proof is similar to that of Theorem 1, so here we skip it to save paper space.  $\square$

**Example 3.** Fig. 6 is an example to demonstrate the SCR-NTs of undirected and directed arbitrary structures. Fig. 7 is an example of the negotiation process of  $a_4$  to implement task  $t$ . For the reason of saving space, we do not express the negotiation process in detail.

### 3 TASK ALLOCATION TO MEET THE CONTEXTUAL RESOURCE DISTRIBUTION

#### 3.1 Contextual Resource Enrichment Factor

An agent will be more resource predominant if its contextual agents have more resources. Let there be an agent  $a_i$ , the set of agents within its physical context is  $PC_i$  and the set of agents within its social context is  $SC_i$ . Obviously, every agent within  $PC_i$  or  $SC_i$  will contribute differently to the resource predominance of  $a_i$ ; the contribution of an agent within  $PC_i$  or  $SC_i$  to agent  $a_i$  is determined by the physical or social distance between such agent and  $a_i$ . Now, we have the concepts of physically contextual enrichment factor and socially contextual enrichment factor.

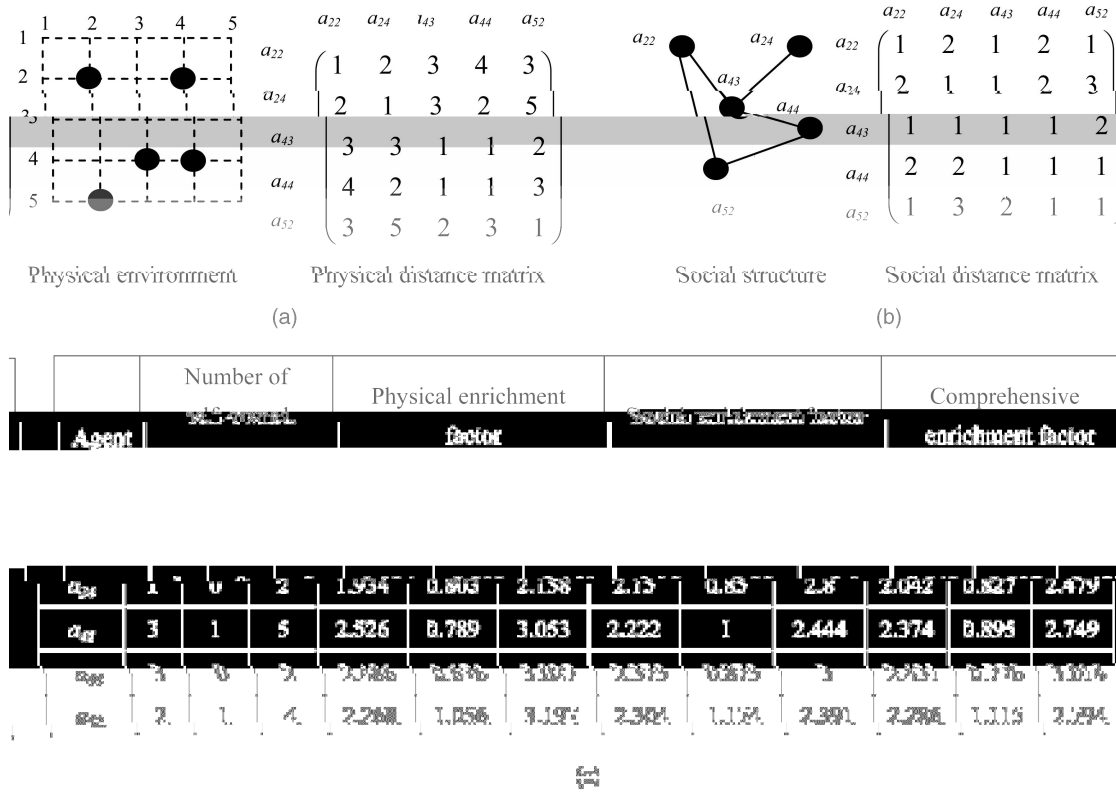


Fig. 8. An example for computing the contextual resource enrichment factors of agents, where  $PC$ s and  $SC$ s of every agent are both the whole agent set  $A: \{a_{22}, a_{24}, a_{43}, a_{44}, a_{52}\}$ . For the reason of simplicity, we can let  $\lambda_s = \lambda_p = 0.5$ . (a) Physical context. (b) Social context. (c) The contextual resource enrichment factors

**Definition 5.** The physically contextual enrichment factor of agent  $a_i$  for resource  $r_k$  is

$$\Phi_i(k) = \sum_{a_j \in PC_i} \left( n_j(k) \cdot \frac{1/d_{ij}^p}{\sum_{a_j \in PC_i} 1/d_{ij}^p} \right), \quad (4)$$

where  $n_j(k)$  is the number of resource  $r_k$  owned by agent  $a_j$ ,  $d_{ij}^p$  is the physical distance between  $a_i$  and  $a_j$ ;  $a_i \in PC_i$ .

**Definition 6.** The socially contextual enrichment factor of agent  $a_i$  for resource  $r_k$  is

$$\Psi_i(k) = \sum_{a_j \in SC_i} \left( n_j(k) \cdot \frac{1/d_{ij}^s}{\sum_{a_j \in SC_i} 1/d_{ij}^s} \right), \quad (5)$$

where  $d_{ij}^s$  is the social distance between agents  $a_i$  and  $a_j$ . We can see that  $d_{ij}^s$  denotes the contribution weight of agent  $a_j$  to the enrichment factor of  $a_i$ , and  $d_{ij}^s$  appears both in the numerator and denominator in (5); thus, we can abstract  $d_{ij}^s$  into a natural number. If two agents are adjacent with each other in the interaction structure, they can make resource negotiation directly and their social distance can be set to 1; therefore, the social distance between two agents can be denoted by the shortest path length in the interaction structure.

**Definition 7.** The comprehensive contextual enrichment factor of agent  $a_i$  for resource  $r_k$  is determined corporately by the physically and socially contextual enrichment factors:

$$\begin{aligned} \xi_i(k) &= \lambda_p \Phi_i(k) + \lambda_s \Psi_i(k) \\ &= \lambda_p \sum_{a_j \in PC_i} \left( n_j(k) \cdot \frac{1/d_{ij}^p}{\sum_{a_j \in PC_i} 1/d_{ij}^p} \right) \\ &\quad + \lambda_s \sum_{a_j \in SC_i} \left( n_j(k) \cdot \frac{1/d_{ij}^s}{\sum_{a_j \in SC_i} 1/d_{ij}^s} \right), \end{aligned} \quad (6)$$

where  $\lambda_p$  and  $\lambda_s$  are used to determine the relative importance of the two kinds of contexts in the contextual enrichment factor of an agent,  $\lambda_p + \lambda_s = 1$ .

For an agent, the higher its contextual resource enrichment factor to one kind of resource is, the higher is its chance to obtain enough of such kind of resource in the system.

**Example 4.** Fig. 8 is an example of contextual resource enrichment factors of agents.

### 3.2 Contextual Resource-Based Task Allocation

The agents are complex with multiple resources related to the multiple tasks they implement in the complex systems. An optimal allocation in a complex system is to maximize the dependability that the tasks can obtain enough resources to be implemented.

For example, in Fig. 8, let there be a task that needs resource  $r_1$ . If we implement the task allocation based on the physically contextual resource distribution, we should allocate the task to agent  $a_{43}$ ; if we implement the task

TABLE 1  
An Example of Task Allocation According to the Comprehensive Enrichment Factor

| Task  | Required resources and number | ERES                         |                                                    |                                                    | MIFS                         |                                                    |                                                    | AAS                          |                                                    |                                                    |
|-------|-------------------------------|------------------------------|----------------------------------------------------|----------------------------------------------------|------------------------------|----------------------------------------------------|----------------------------------------------------|------------------------------|----------------------------------------------------|----------------------------------------------------|
|       |                               | PA                           | CA                                                 |                                                    | PA                           | CA                                                 |                                                    | PA                           | CA                                                 |                                                    |
|       |                               |                              | PN                                                 | SN                                                 |                              | PN                                                 | SN                                                 |                              | PN                                                 | SN                                                 |
| $t_1$ | $3r_1, 1r_3^*, 4r_2$          | $a_{44}$<br>$\{3r_1, 1r_3\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ | $a_{44}$<br>$\{3r_1, 1r_3\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ | $a_{44}$<br>$\{3r_1, 1r_3\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(2r_2)$ |
| $t_2$ | $2r_3, 3r_1, 3r_2^*$          | $a_{44}$<br>$\{2r_3, 3r_1\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ | $a_{22}$<br>$\{2r_3, 3r_1\}$ | $a_{24}$<br>$\{2r_3, 3r_1\}$                       | $a_{43}$<br>$\{2r_3, 3r_1\}$                       | $a_{44}$<br>$\{2r_3, 3r_1\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ |
| $t_3$ | $2r_2^*, 3r_1, 1r_3$          | $a_{22}$<br>$\{2r_2, 2r_1\}$ | $a_{24}$<br>$\{1r_1, 1r_2\}$                       | $a_{43}$<br>$\{1r_1, 1r_2\}$                       | $a_{22}$<br>$\{2r_2, 2r_1\}$ | $a_{24}$<br>$\{1r_1, 1r_2\}$                       | $a_{43}$<br>$\{1r_1, 1r_2\}$                       | $a_{44}$<br>$\{3r_1, 1r_3\}$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ | $a_{43}(1r_2)$<br>$a_{52}(1r_2)$<br>$a_{22}(1r_2)$ |

\* The most important resource. PA: principal agent; CA: cooperated agent; PN: physical negotiation; and SN: social negotiation.

allocation based on the socially contextual resource distribution, we should allocate the task to agent  $a_{44}$ ; if we implement the task allocation based on the comprehensive contextual resource distribution, we should allocate the task to agent  $a_{44}$ .

From the above example, we can see that it is easy to make definite effective allocation if the task only requires one kind of resources. However, if a task needs many kinds of resources, then how can we implement the allocation? For example, in Fig. 8, we let a task need resource  $r_1$  and  $r_2$ . If we implement the task allocation based on comprehensive contextual resource distribution,  $a_{44}$  has the highest enrichment factor for  $r_1$  and  $a_{22}$  has the highest enrichment factor for  $r_2$ . Then, which one of  $a_{44}$  or  $a_{22}$  should be allocated with the task? To solve this problem, we can design the allocation method for the task that requires more than one kind of resources as follows:

When a task requires more than one resource, we should assign an agent to act as the *principal one* (i.e., the initiator agent within the negotiation), which will initially negotiate with other agents for the resources required by the task; then, the set of all agents that provide resources for the task is the allocated agents. To determine the principal agent, we set some criterions as follows:

1. *First Required Resource-First Satisfy (FRFS)*. When a task requires many resources, it may call each resource sequentially. Now, we can design the criterion of FRFS, i.e., the agent that has the highest enrichment factor for the first called resource should be allocated as the principal one of that task. Let there be a task  $t$ , the set of resources called by task  $t$  orderly is  $\{n_1r_1, n_2r_2, \dots, n_nr_n\}$ ;  $n_i$  denotes the required number of resource  $r_i$ . So, we will allocate  $t$  to the agent  $a_j$ , which has the highest enrichment factor for  $r_1$ , i.e., the highest  $\Phi_j(1)$ ,  $\Psi_j(1)$ , or  $\xi_j(1)$ . For example, in Fig. 8, if the called resource sequence of a task is  $\{r_2, r_1, r_2, r_3\}$  and  $a_{22}$  has the highest contextual resource enrichment factor for resource  $r_2$ ,  $a_{22}$  will be assigned as the principal one for such task.
2. *Most Important Resource-First Satisfy (MIFS)*. When a task requires many resources, there may be one resource that is the most important for implementing that task. Now, let there be a task  $t$ , the set of resources

called by task  $t$  orderly is  $\{n_1r_1, n_2r_2, \dots, n_nr_n\}$ ; if  $r_i$  is the most important resource for implementing  $t$ , we will allocate  $t$  to agent  $a_j$ , which has the highest enrichment factor for resource  $r_i$ , i.e., the highest  $\Phi_j(i)$ ,  $\Psi_j(i)$ , or  $\xi_j(i)$ . For example, in Fig. 8, if the called resource sequence of a task  $t$  is  $\{r_2, r_1, r_2, r_3\}$  and  $r_1$  is the most important for the implementation of  $t$ ,  $a_{44}$  will be assigned as the principle one for  $t$  since  $a_{44}$  has the highest contextual enrichment factor for resource  $r_1$ .

3. *All Resources-Averagely Satisfy (AAS)*. When a task  $t$  requires resources  $\mathbf{F}_t$ , we can allocate the task to the agent, which has the highest average contextual enrichment factor for all resources in  $\mathbf{F}_t$ . Now, let  $\mathbf{F}_t = \{n_1r_1, n_2r_2, \dots, n_nr_n\}$ , we will allocate task  $t$  to the following agent (according to the comprehensive contextual resource enrichment factor  $\xi_j(i)$ ):

$$a_* = \arg \max_{a_j \in A} \left( \frac{1}{|\mathbf{F}_t|} \sum_{r_i \in \mathbf{F}_t} \xi_j(i) \right). \quad (7)$$

Therefore, our **task allocation process** is explained as follows: 1) Assign task  $t$  to a principal agent according to the above three criterions, now it is assumed that the principal agent is  $a_*$ ; 2) let the set of resources required by task  $t$  be  $\mathbf{F}_t$ , the resources owned by agent  $a_*$  be  $\mathbf{F}_{a_*}$ , and  $\mathbf{F}_{a_*}^t = \mathbf{F}_t - \mathbf{F}_{a_*}$ , now agent  $a_*$  will behave as the initiator agent and negotiate with other agents within its physical context or social context according to the methods presented in Section 2; and 3) let the set of agents that will provide the requested resources to  $a_*$  be  $A'$ , thus task  $t$  will be finally implemented by the allocated agent set:  $A_t = \{a_*\} \cup A'$ .

**Example 4 (continue).** We use the example in Fig. 8 to demonstrate the task allocation, as shown in Table 1. For example, task  $t_2$  needs three kinds of resources:  $2r_3$ ,  $3r_1$ , and  $3r_2$ ; if we use MIFS to determine the principal agent,  $a_{22}$  will be selected and provide  $2r_1$  and  $3r_2$  for the task; so now  $a_{22}$  will negotiate with other contextual agents for  $2r_3$  and  $1r_1$ ; if  $a_{22}$  negotiates with other agents within its physical context, the agent set  $\{a_{24}\}$  will be allocated; if  $a_{22}$  negotiates with other agents within its social context, the agent set  $\{a_{43}\}$  will be allocated.

#### 4 CONTEXT-ASSOCIATED LOAD BALANCING FOR MULTIPLE TASKS

According to the model in Section 3, an agent may have more tasks to queue if it has higher contextual resource enrichment factor. Therefore, we should deal with the *load balancing* while there are multiple tasks within the complex system.

Generally, the performance of load balancing is mainly determined by the waiting time of the task. According to Liu et al. [10], the effect of measures on load balancing is reflected by the number and size of task teams on agents; and we simply consider that the waiting time is only related to the length of the task team. Let the allocated agent set of task  $t$  be  $A_t$  and the set of resources required by  $t$  be  $R_t$ . We can denote the team of tasks that queue for the resource  $r_k$  of agent  $a_i$  as  $Q_{ik}$ , and the size of  $Q_{ik}$  as  $s_{ik}$ . If task  $t$  calls its requested resources concurrently, the waiting time of task  $t$  will be determined by the maximum size of the queues for its required resources; if task  $t$  calls its requested resources serially, the waiting time of task  $t$  will be determined by the total sizes of the queues for its required resources. Therefore, we can define the waiting time of a task as

$$w_t = \max_{\forall r_i \in R_t, \forall a_k \in A_t} (s_{ik}), \quad \text{or} \quad w_t = \sum_{\forall r_i \in R_t, \forall a_k \in A_t} (s_{ik}). \quad (8)$$

Now, if there are multiple tasks that arrive at the complex system, the set of those multiple tasks is  $T$ , thus we can define the global load balancing performance of the system as

$$\tilde{w} = \frac{1}{|T|} \sum_{t \in T} w_t. \quad (9)$$

Therefore, our goal of load balancing is to reduce the average size of the queues for all resources and all agents. In the previous research work on load balancing [10], [11], [28], an agent's probability to be allocated new tasks will be reduced if it has already undertaken too many tasks; thus, the number of undertaken tasks of an agent will only influence the probability of itself to be allocated new tasks in the task allocation.

However, an agent will negotiate with its contextual agents for resources; thus, if an agent has already been allocated with too many tasks, the probabilities of its contextual agents to accept new tasks should also be reduced. Thus, we will develop the load balancing method also based on the contextual resource distribution. If an agent,  $a$ , is allocated with some tasks, it is not only  $a$  itself but also the agents in the context of  $a$  will be reduced the possibilities to accept new tasks in the future. Let  $s_{ik}$  be the size of team where tasks queue for the resource  $r_k$  of agent  $a_i$ , the contextual enrichment factors of agents within the physical and social contexts of  $a_i$  will be changed as

$$\forall a_j \in PC_i, \Phi_j^*(k) = \Phi_j(k) - \sigma\left(\frac{s_{ik}}{d_{ij}^p}\right), \quad (10)$$

$$\forall a_j \in SC_i, \Psi_j^*(k) = \Psi_j(k) - \sigma\left(\frac{s_{ik}}{d_{ij}^s}\right), \quad (11)$$

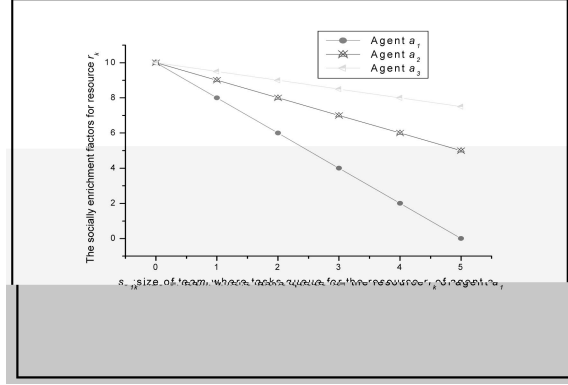


Fig. 9. Numerical simulation for the contextual resource enrichment factor modification.

where  $\sigma$  is a monotonously increasing function;  $d_{ij}^p$  is the physical distance between agents  $a_i$  and  $a_j$ ,  $a_i \in PC_i$ ;  $d_{ij}^s$  is the social distance between agents  $a_i$  and  $a_j$ ,  $a_i \in SC_i$ .

**Example 4 (numerical simulations).** Let there be three agents in a social context,  $\{a_1, a_2, a_3\}$ , the social distance from  $a_1$  to  $a_2$  is 1, the social distance from  $a_1$  to  $a_3$  is 2, for simplicity, we can let the social distance from  $a_1$  to itself be 0.5; Let the size of team where tasks queue for the resource  $r_k$  of agent  $a_1$ ,  $s_{1k}$ , be 0 initially, and the socially contextual enrichment factors of the three agents to  $r_k$  be all 10 initially. Now, the value of  $s_{1k}$  increases with the step of 1; from Fig. 9, we can see that the enrichment factors of three agents will decrease accordingly; and the nearer to  $a_1$ , the more rapidly the agent's enrichment factor decreases.

#### 5 VALIDATIONS AND ANALYSES

To validate the correctness and effect of our task allocation and load balancing model based on contextual resource negotiation, we make a series of case simulations. We can define the task in the simulation test as follows:

It is assumed that each resource of an agent can only be obtained by one task at the same time. Let the task is allocated to a series of agents, and the task creates a token that will be sent from the first agent to the next and so on along the agent series until it arrives at the last agent and obtains the required resources. Thus, the execution of task is given as follows: 1) First, the token is dead, 2) when the token is newly received by an allocated agent, then it will be dead; only when it can obtain the enough required resources from its now inhabited agent, the token can be activated and sent to the next allocated agent, and 3) such process will continue until the token visits all allocated agents and is active at last.

For example, let task  $t_1$  be allocated to " $a_{44}(3r_1, 1r_3)$ ,  $a_{22}(3r_2)$ ,  $a_{43}(1r_2)$ ," so the execution of  $t_1$  is given as follows: 1) At first, a dead token is created in  $a_{44}$ , when  $t_1$  obtains " $3r_1, 1r_3$ " from  $a_{44}$ , the token is activated and sent to  $a_{22}$ , then resources " $3r_1, 1r_3$ " are released; 2) now,  $a_{22}$  receives the token and makes it a dead one, when  $t_1$  obtains " $3r_2$ " from  $a_{22}$ , the token is activated and sent to  $a_{43}$ , then resources " $3r_2$ " are released; 3) now,  $a_{43}$  receives the token and makes it a dead one; when  $t_1$  obtains " $1r_2$ " from  $a_{43}$ , the token is activated and now the task is finished, and resources " $1r_2$ " are released. Therefore, let  $g_{ai}$  denote the time of "getting required resources" from agent  $a_i$ ,  $c_{ai \rightarrow aj}$

TABLE 2  
The Task Allocation Processes in the SRM Model

| FRFS (First required resource-firstly satisfy)                                                                | MIFS (Most important resource-firstly satisfy)                                                                | AAS (All resources-averagely satisfy)                                                                                                             |
|---------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|
| 1). $A_i = \{\}$ ;<br>2). While $R_i \neq \{\}$ :<br>2.1). $r_*$ be the first required resource<br>in $R_i$ ; | 1). $A_i = \{\}$ ;<br>2). While $R_i \neq \{\}$ :<br>2.1). $r_*$ be the most important resource<br>in $R_i$ ; | 1). $A_i = \{\}$ ;<br>2). While $R_i \neq \{\}$ :<br>2.1). $a_* = \arg \max_{a_i \in A} \left( \frac{1}{ R_i } \sum_{r \in R_i} n_j(i) \right)$ ; |
| 2.2). $A_i = A_i \cup \{r_*\}$ ;<br>$\cap A_i \cap D = D \cap D$ ;                                            | 2.2). $A_i = A_i \cup \{r_*\}$ ;<br>$\cap A_i \cap D = D \cap D$ ;                                            | 2.2). $A_i = A_i \cup \{a_*\}$ ;<br>$\cap A_i \cap D = D \cap D$ ;                                                                                |
| 2.3). $R_i = R_i - R_*$ ;                                                                                     | 2.3). $R_i = R_i - R_*$ ;                                                                                     | 2.3). $R_i = R_i - R_*$ ;                                                                                                                         |

denote the communication time from  $a_i$  to  $a_j$ , then the execution time of  $t_i$  is

$$E_{t1} = g_{a44} + c_{a44 \rightarrow a22} + g_{a22} + c_{a22 \rightarrow a43} + g_{a43}. \quad (12)$$

From above, we can see that the execution time of a task is determined by the resource access time (i.e., the waiting time of the task described in Section 4) and the communication time among allocated agents. Therefore, the task team on an agent is longer, the time of “getting resource” is longer, and that leads the execution time of task to become longer; on the other hand, the distance among allocated agents is longer, the time of “communication time” will be longer, and that also leads the execution time of task to become longer.

### 5.1 Comparison between Contextual Resource-Based Task Allocation and Self-Owned Resource-Based Task Allocation

In this section, we will validate the correctness of our task allocation model, so we will compare the performances of the following two models: 1) Contextual resource-based task allocation model, CRM and 2) Self-owned resource-based task allocation model, SRM. In the SRM, the task allocation is implemented according to the self-owned resources of agents themselves, which is always used in the previous related work. Now, we introduce the SRM model briefly.

When a task requires more than one resource, we can also use the three criteria described in Section 3.2. Now, let there be a task  $t$ , the set of resources called by task  $t$  is  $P_t = \{n_1 r_1, n_2 r_2, \dots, n_n r_n\}$ ,  $n_j(i)$  denotes the number of  $r_i$  owned by agent  $a_j$ ,  $P_i$  denotes the set of resources owned

by agent  $a_i$ , then the task allocation processes of SRM are shown in Table 2.

Then, we make a series of case simulations to test the two models. In the simulations, the agent number is 200, the physical distribution and social structure can be set randomly. We can use SRM and CRM models to make task allocation; the allocated agents will execute the tasks, then the total execution time of tasks is tested. The results are shown in Fig. 10.

From the results, we can obtain the following: 1) when CRM model is used, the allocated agents will always incline to be located within the near physical contexts or social contexts, so the communication time will be reduced; however, the allocated agents in SRM model will always be distributed through the system, so the communication time among agents will incline to be more than the one of CRM model. Therefore, the task execution time of CRM model is always less than the one of the SRM model and 2) while the number of tasks increases, the communication time will also increase; so the difference between the two models will increase accordingly.

Therefore, we can conclude that the CRM model can reduce the total communication time among allocated agents so as to reduce the total task execution time compared to SRM, especially while the number of tasks is large.

### 5.2 Comparison between Contextual Resource-Based Load Balancing and Self-Owned Resource-Based Load Balancing

Now, we will compare the contextual resource-based load balancing and the self-owned resource-based load balancing.

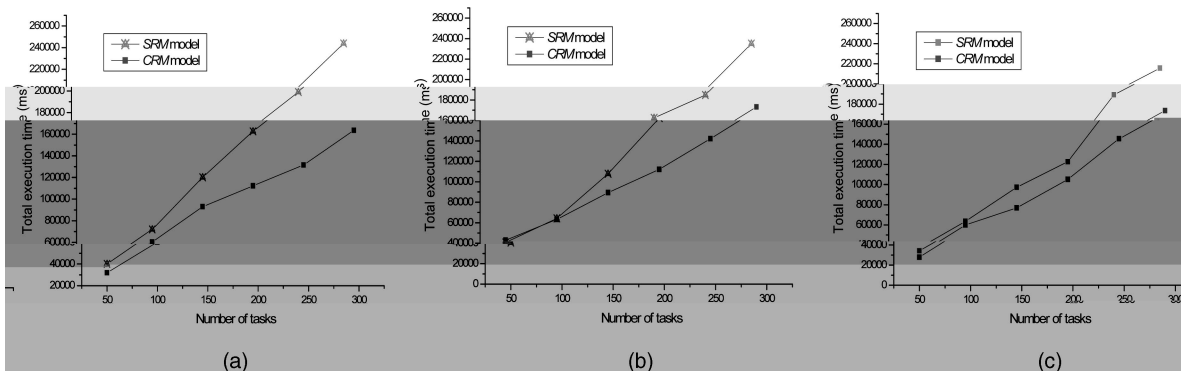


Fig. 10. Execution time comparison between SRM and CRM models. (a) FRFS. (b) MIFS. (c) AAS.

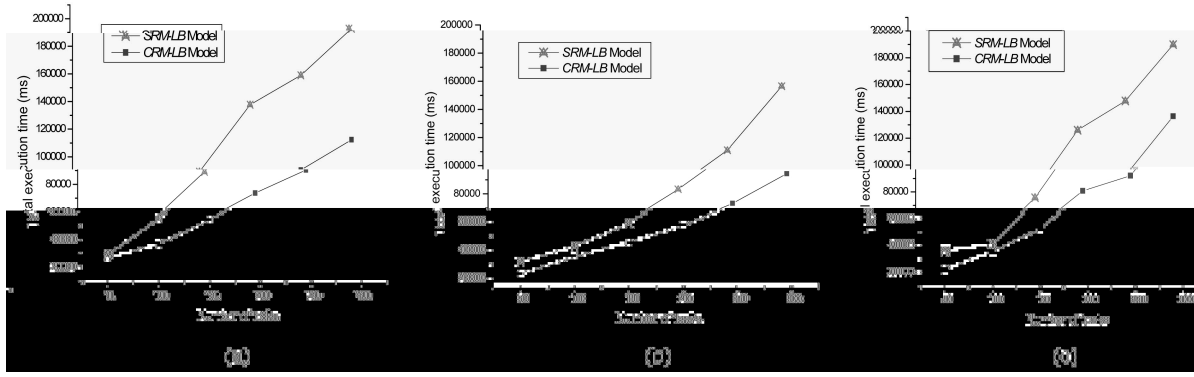


Fig. 11. Execution time comparison between *SRM-LB* and *CRM-LB* models. (a) FRFS. (b) MIFS. (c) AAS.

In Section 4, we have addressed the contextual resource-based task allocation with load balancing (*CRM-LB*), now we briefly introduce the self-owned resource-based task allocation with load balancing (*SRM-LB*).

Let  $s_{jk}$  be the size of teams where tasks queue for the resource  $r_k$  of agent  $a_j$ , the number of  $r_k$  owned by agent  $a_j$  is  $n_j(k)$ , so the self-owned resource enrichment factor of agent  $a_j$  on  $r_k$ ,  $\varphi_j(k)$ , should be changed as (13) when we consider the load balancing:

$$\varphi_j(k) = n_j(k) - f(s_{jk}), \quad (13)$$

where  $f$  is a monotonously increasing function. Therefore, while an agent is allocated with more tasks, its probability to obtain new task in the future will be reduced. When a task  $t$  is allocated to some agents that are  $A_t$ , all agents in  $A_t$  should modify their self-owned resource enrichment factor according to (13).

We make some case simulations to test the two models. In the simulations, the agent number is 200, the physical distribution and social structure can be set randomly. We can use the *CRM-LB* model and *SRM-LB* model to make the task allocation; the allocated agents will execute the tasks, then the total execution time for the tasks is tested. The results are shown in Fig. 11.

From the results, we can obtain the following:

1. The total execution time in *CRM-LB* is less than the one in *SRM-LB*, since the *CRM-LB* model can reduce the total communication time among allocated

agents so as to reduce the total task execution time that is better than *SRM-LB*, especially while the number of tasks is large.

2. The gap between the two models in Fig. 11 is bigger than the one in Fig. 10, so the load balancing in *CRM-LB* outperforms the one in *SRM-LB*. We conclude that *CRM-LB* is better suited for the characteristics of complex software systems, since *CRM-LB* adjusts the contextual resource enrichment factors of allocated agents themselves as well as their contextual agents, but *SRM-LB* only adjusts the self-owned resource enrichment factors of allocated agents themselves.

### 5.3 Comparison between *CRM-LB* and *CRM*

We now compare *CRM-LB* and the contextual resource-based task allocation *without* load balancing (*CRM*). In the simulations, the agent number is 200, the physical distribution and social structure can be set randomly. We can use the *CRM-LB* and *CRM* models to make the task allocation; the allocated agents will execute the task, then the total execution time for the tasks is tested. The results are shown in Fig. 12.

From the results, we can see that *CRM-LB* outperforms *CRM*; while the task number increases, the *CRM-LB* will outperform *CRM* more and more. Therefore, our load balancing model can make an effective load balancing and reduce the task waiting time for resources while there are multiple tasks in the complex systems.

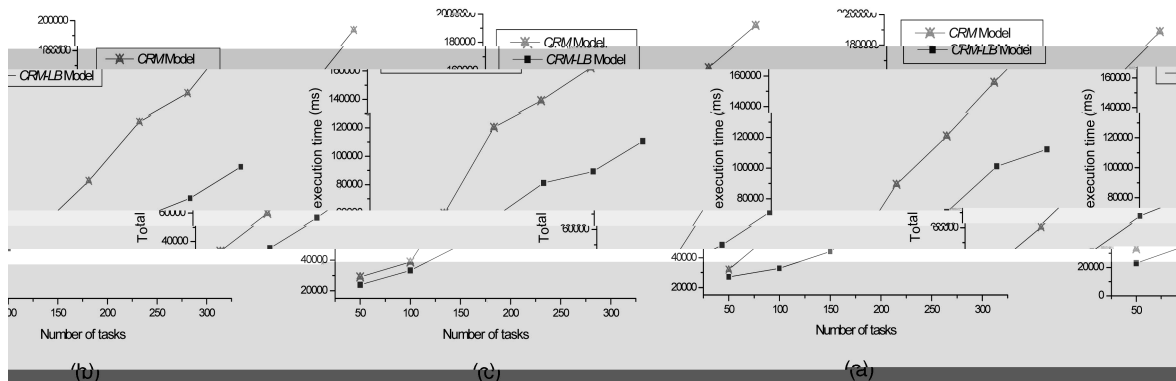


Fig. 12. Execution time comparison between *CRM* and *CRM-LB* models. (a) FRFS. (b) MIFS. (c) AAS.

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